

# Multiple Choice Test

## Gauss-Seidel Method of Solving Simultaneous Linear Equations

1. A square matrix  $[A]_{n \times n}$  is diagonally dominant if

$$(A) \quad |a_{ii}| \geq \sum_{\substack{j=1 \\ i \neq j}}^n |a_{ij}|, \quad i = 1, 2, \dots, n$$

$$(B) \quad |a_{ii}| \geq \sum_{\substack{j=1 \\ i \neq j}}^n |a_{ij}|, \quad i = 1, 2, \dots, n \quad \text{and} \quad |a_{ii}| > \sum_{\substack{j=1 \\ i \neq j}}^n |a_{ij}|, \quad \text{for any } i = 1, 2, \dots, n$$

$$(C) \quad |a_{ii}| \geq \sum_{j=1}^n |a_{ij}|, \quad i = 1, 2, \dots, n \quad \text{and} \quad |a_{ii}| > \sum_{j=1}^n |a_{ij}|, \quad \text{for any } i = 1, 2, \dots, n$$

$$(D) \quad |a_{ii}| \geq \sum_{j=1}^n |a_{ij}|, \quad i = 1, 2, \dots, n$$

2. Using  $[x_1 \ x_2 \ x_3] = [1 \ 3 \ 5]$  as the initial guess, the value of  $[x_1 \ x_2 \ x_3]$  after three iterations in Gauss-Seidel method for

$$\begin{bmatrix} 12 & 7 & 3 \\ 1 & 5 & 1 \\ 2 & 7 & -11 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 2 \\ -5 \\ 6 \end{bmatrix}$$

is

- (A) [-2.8333 -1.4333 -1.9727]
- (B) [1.4959 -0.90464 -0.84914]
- (C) [0.90666 -1.0115 -1.0242]
- (D) [1.2148 -0.72060 -0.82451]

3. To ensure that the following system of equations,

$$2x_1 + 7x_2 - 11x_3 = 6$$

$$x_1 + 2x_2 + x_3 = -5$$

$$7x_1 + 5x_2 + 2x_3 = 17$$

converges using Gauss-Seidel Method, one can rewrite the above equations as follows:

$$(A) \begin{bmatrix} 2 & 7 & -11 \\ 1 & 2 & 1 \\ 7 & 5 & 2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 6 \\ -5 \\ 17 \end{bmatrix}$$

$$(B) \begin{bmatrix} 7 & 5 & 2 \\ 1 & 2 & 1 \\ 2 & 7 & -11 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 17 \\ -5 \\ 6 \end{bmatrix}$$

$$(C) \begin{bmatrix} 7 & 5 & 2 \\ 1 & 2 & 1 \\ 2 & 7 & -11 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 6 \\ -5 \\ 17 \end{bmatrix}$$

(D) The equations cannot be rewritten in a form to ensure convergence.

4. For  $\begin{bmatrix} 12 & 7 & 3 \\ 1 & 5 & 1 \\ 2 & 7 & -11 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 22 \\ 7 \\ -2 \end{bmatrix}$  and using  $[x_1 \ x_2 \ x_3] = [1 \ 2 \ 1]$  as the initial guess, the values of  $[x_1 \ x_2 \ x_3]$  are found at the end of each iteration as

Iteration #	$x_1$	$x_2$	$x_3$
1	0.41666	1.1166	0.96818
2	0.93989	1.0183	1.0007
3	0.98908	1.0020	0.99930
4	0.99898	1.0003	1.0000

At what first iteration number would you trust at least 1 significant digit in your solution?

- (A) 1
- (B) 2
- (C) 3
- (D) 4

5. The algorithm for the Gauss-Seidel Method to solve  $[A][X] = [C]$  is given as follows for using  $n_{max}$  iterations. The initial value of  $[X]$  is stored in  $[X]$ .

```
(A) Sub Seidel(n, a, x, rhs, nmax)
    For k = 1 To nmax
    For i = 1 To n
    For j = 1 To n
    If (i <> j) Then
    Sum = Sum + a(i, j) * x(j)
    endif
    Next j
    x(i) = (rhs(i) - Sum) / a(i, i)
    Next i
    Next k
End Sub
```

```
(B) Sub Seidel(n, a, x, rhs, nmax)
    For k = 1 To nmax
    For i = 1 To n
    Sum = 0
    For j = 1 To n
    If (i <> j) Then
    Sum = Sum + a(i, j) * x(j)
    endif
    Next j
    x(i) = (rhs(i) - Sum) / a(i, i)
    Next i
    Next k
End Sub
```

```
(C) Sub Seidel(n, a, x, rhs, nmax)
    For k = 1 To nmax
    For i = 1 To n
    Sum = 0
    For j = 1 To n
    Sum = Sum + a(i, j) * x(j)
    Next j
    x(i) = (rhs(i) - Sum) / a(i, i)
    Next i
    Next k
End Sub
```

```

(D) Sub Seidel(n, a, x, rhs, nmax)
    For k = 1 To nmax
    For i = 1 To n
    Sum = 0
    For j = 1 To n
    If (i <> j) Then
    Sum = Sum + a(i, j) * x(j)
    endif
    Next j
    x(i) = rhs(i) / a(i, i)
    Next i
    Next k
End Sub

```

6. Thermistors measure temperature, have a nonlinear output and are valued for a limited range. So when a thermistor is manufactured, the manufacturer supplies a resistance vs. temperature curve. An accurate representation of the curve is generally given by

$$\frac{1}{T} = a_0 + a_1 \ln(R) + a_2 \{\ln(R)\}^2 + a_3 \{\ln(R)\}^3$$

where T is temperature in Kelvin, R is resistance in ohms, and  $a_0, a_1, a_2, a_3$  are constants of the calibration curve.

Given the following for a thermistor

<b>R</b>	<b>T</b>
<b>ohm</b>	<b>°C</b>
1101.0	25.113
911.3	30.131
636.0	40.120
451.1	50.128

the value of temperature in °C for a measured resistance of 900 ohms most nearly is

- (A) 30.002
- (B) 30.472
- (C) 31.272
- (D) 31.445